

SECTION A · PURE MATHEMATICS

Pure Mathematics · 50 marks · Questions 1 – 9

Answer ALL questions in Sections A and B. The paper lasts 2 hours and carries 100 marks: Section A is worth 50 marks and Section B is worth 50 marks. The first questions in each section are one-mark multiple-choice items. Show all necessary working. Unless a question says otherwise, give non-exact numerical answers to three significant figures.

1. Find the magnitude of the vector $2\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}$. Circle the correct answer. [1 mark]

- A 49
- B 7
- C 48
- D 11

2. The graph of $y = f(x)$ is transformed to the graph of $y = f(6x + 1)$. Which sequence of transformations produces this? Circle your answer. [1 mark]

- A a stretch in the x-direction with scale factor $\frac{1}{6}$, then a translation of 1 unit in the negative x-direction
- B a translation of 1 unit in the negative x-direction, then a stretch in the x-direction with scale factor 6
- C a translation of 1 unit in the positive x-direction, then a stretch in the x-direction with scale factor $\frac{1}{6}$
- D a translation of 1 unit in the negative x-direction, then a stretch in the x-direction with scale factor $\frac{1}{6}$

3. A point on the curve $y = \ln(2x^2 + 5)$ has $x = 1$. Work out the gradient of the curve at this point. Circle the correct answer. [1 mark]

- A $\frac{1}{7}$
- B 4
- C $\frac{4}{7}$
- D $\frac{2}{7}$

THE WORKED ANSWERS TO THOSE 3 QUESTIONS

1. Find the magnitude of the vector $2\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}$. Circle the correct answer. [1 mark] [Vectors]

Correct answer: B — 7

- Magnitude = $\sqrt{(\text{sum of squares of the components})} = \sqrt{(2^2 + 6^2 + 3^2)}$.
- $= \sqrt{49} = 7$.
- Marks (TPH scheme): B1 [AO1]. The other options come from common slips: a wrong formula, a wrong sign or a missed step.

LOS: Pure Mathematics · Vectors

KEY TAKEAWAY

Magnitude is the square root of the sum of the squared components.

2. The graph of $y = f(x)$ is transformed to the graph of $y = f(6x + 1)$. Which sequence of transformations produces this? Circle your answer. [1 mark] [Functions and graphs]

Correct answer: D — a translation of 1 unit in the negative x-direction, then a stretch in the x-direction with scale factor $\frac{1}{6}$

- Start from $y = f(x)$. Translating 1 unit in the negative x-direction gives $y = f(x + 1)$.
- Replacing x by $6x$ in that equation gives $y = f(6x + 1)$, and replacing x by $6x$ is a stretch in the x-direction with scale factor $\frac{1}{6}$.
- So the sequence is a translation then a stretch, as stated.
- Marks (TPH scheme): B1 [AO1]. The other options come from common slips: a wrong formula, a wrong sign or a missed step.

LOS: Pure Mathematics · Functions and graphs

KEY TAKEAWAY

Apply the changes to x in the same order as they are built: $x \rightarrow x + t$ first, then $x \rightarrow sx$.

3. A point on the curve $y = \ln(2x^2 + 5)$ has $x = 1$. Work out the gradient of the curve at this point. Circle the correct answer. [1 mark] [Differentiation]

Correct answer: C — $\frac{4}{7}$

- Use the chain rule: $dy/dx = (\text{derivative of the inside}) \div (\text{the inside}) = 4x \div (2x^2 + 5)$.
- At $x = 1$ the gradient is $\frac{4}{7}$.
- Marks (TPH scheme): B1 [AO1]. The other options come from common slips: a wrong formula, a wrong sign or a missed step.

LOS: Pure Mathematics · Differentiation

KEY TAKEAWAY

The derivative of $\ln$ of a function is the derivative of the function divided by the function.